

Soliton

Vision for a Better World

Not to be circulated outside

Computer Vision with Machine Learning

PSG Tech - 2018



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Day 2

Had Colorful Dreams..?

Agenda

Session I

- Linear Regression
- Logistic Regression
- Over / Under Fitting
- SVM
- Other ML Techniques

Linear Classifier

A line should classify the data

But, How do I come up with a Line which separates both the classes of data optimally?

• Nut





2 ML Problems





Let's Digress into Regression



Gradient Descent

- The magnitude of the update is proportional to the error term (y(i) - h θ (x (i)))
- If a training example on which our prediction nearly matches the actual y (i), there is little need to change the parameters



Repeat until convergence {

$$\begin{aligned} \theta_{j} &:= \theta_{j} + \alpha \sum_{i=1}^{m} \left(y^{(i)} - h_{\theta}(x^{(i)}) \right) x_{j}^{(i)} & \text{(for every } j\text{)}. \end{aligned} \\ \begin{aligned} & \text{Batch Gradient} & \text{for } i=1 \text{ to } \text{m}, \\ & \text{Descent} & \text{for } i=1 \text{ to } \text{m}, \\ & \text{Stochastic Gradient} & \theta_{j} &:= \theta_{j} + \alpha \left(y^{(i)} - h_{\theta}(x^{(i)}) \right) x_{j}^{(i)} & \text{(for every } j\text{)}. \\ & & \text{} \end{aligned}$$





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Linear Classifier

A line should classify the data

- Randomly Initialize a Line
- Calculate Error
- Move in a Random Direction
- Recalculate Error
- If Error reduced, move in same direction
- Else move in opposite direction

• Bolt

• Nut





Parts of an ML Algo: ERM





Inference

- Hypothesis space, the set of possible hypotheses it can come up with in order to model the unknown target function by formulating the final hypothesis
- An example (linear function)

$$h(x) = \sum_{i=0}^{n} \theta_i x_i = \theta^T x,$$

Learning

- X Training data Y Labels $h(\theta)$ = Predicted label
 - Cost function => $J(\theta) = h(\theta) y$ [Predicted Actual]

• Update Rule
$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta).$$

Logistic Regression

The Line can be drawn from the learned parameters

 $\theta_0 + \theta_1 X_1 + \theta_2 X_2 = 0$ $X_1 = \theta_0 / \theta_1 + \theta_2 X_2 / \theta_1$





Logistic Regression



Learning

X - Training data Y - Labels $h(\theta)$ = Predicted label

- This can be simplified as $h_{\theta}(x) = g(\theta^T x) = \frac{1}{1 + e^{-\theta^T x}}$
- Cost function $J(\theta) = \frac{1}{2} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) y^{(i)})^2$.
- Update Rule $\theta_j := \theta_j \alpha \frac{\partial}{\partial \theta_j} J(\theta).$

Gradient Descent: Starts with some initial value of θ and repeatedly performs update



Overfitting & Underfitting







Overfitting & Underfitting

How to Fix

- 1. Cross Validation
- 2. Feature selection
- 3. Regularization









All (Wo)Men must Code

Basic ML Notebook

VALAR MORGHULIS



Problems

Why Logistic Regression does not work?



 $\text{Circularity} \rightarrow$



More intelligent classifier

Which of the linear separators is optimal?





Margins

Let's take the Logistic regression example

Among A, B and C which data point would you confidently classify as Bolt?

If the point is far from the separating hyperplane, we may be significantly more confident in our predictions

Find a decision boundary that allows us to make all CORRECT and CONFIDENT predictions



Circularity \rightarrow



SVM

Optimal Margin Classifier

- Examples closest to the separator are support vectors.
- Margin ρ of the separator is the distance between support vectors
 r = (W^TX + b) / ||W||
- Functional Margin $\gamma^{(i)} = y(i) (w^T x + b)$





Nonseparable Data

We learned that SVM is a Linear Classifier

Can SVM classify the given data?





Project data to Higher Dimension





Hyperplane re-projection in 2D

Data in R^3 (separable w/ hyperplane)

1.4 1.4 1.2 1.0 0.8 0.6 0.4 0.2 1.0 0.5 0.0 -0.5 -1.0 -1.0 -0.5 0.0 0.5 1.0 X Label





Demo

Just,

- Project the data into higher Dimension
- Find Hyperplane
- Re-project the Hyperplane back to original dimension





Kernel Trick

It is so simple. Is it True?

Higher Dimensional Projection is Expensive

- Impractical for Large Dimensions
- Huge memory and Computation are required
- Transformation from N dimension to M Dimension is O(N²) expensive

We only need Dot Products ..! Not the High Dimension Data

 $\phi(x) =$

 $K(x, z) = \phi(x)^T \phi(z)$

$$\begin{bmatrix} x_1x_1 \\ x_1x_2 \\ x_1x_3 \\ x_2x_1 \\ x_2x_1 \\ x_2x_2 \\ x_2x_3 \\ x_3x_1 \\ x_3x_2 \\ x_3x_3 \end{bmatrix} .$$

$$K(x,z) = \left(\sum_{i=1}^n x_iz_i\right) \left(\sum_{j=1}^n x_iz_i\right)$$

$$= \sum_{i=1}^n \sum_{j=1}^n x_ix_jz_iz_j$$

$$= \sum_{i,j=1}^n (x_ix_j)(z_iz_j)$$

$$O(N^2) \qquad O(N)$$

Computationally Faster and No extra memory needed



idea

SVM

Find the Hyperplane which optimizes the Functional and Geometric margin iteratively

• Bolt

• Nut





Hands-on is Coming..!



IPython Notebook

Real World Data

In the real world the data may not be Linearly separable

How do we classify the data now?

• Nut





More Features

If I project the same data into 3D / 4D / 5D, etc, can I separate the data Linearly?

Introduce more features for more accurate classification









ML Advice - Diagnostics

		High Variance
Try getting more training examples	Fixes high Variance	
Try a smaller set of features	Fixes high Variance	Test error
Try a larger set of features	Fixes high Bias	Training error
Try changing features (e.g, email header features)	Fixes high Bias	m (training set size)
Run gradient descent for more iterations	Fixes optimization algorithm	High Bias
Try Newton's method	Fixes optimization algorithm	Test error
Use a different value for $\boldsymbol{\lambda}$	Fixes optimization objective	Training error Desired performance
Try using an SVM	Fixes optimization objective	
		m (training set size)



ML Advice

Rule #1: Plot the Data

Questions to ask:

Is the Algorithm converging?

Are you optimizing the right function?

Is the value for λ is correct?

Is the value for C is correct?

Are initial parameters correct?

Error Analysis

- Helps to understand how much error is attributable to each component?
- Helps to identify Poor components by which we can improve performance
- List down accuracy **DROP** after introducing each component.
- Plug in ground-truth for each component, and see how accuracy changes

Ablative Analysis

- Helps to understand how each component in the system helps to achieve final better accuracy
- Helps to identify the less contributing component so they can be removed
- List down what is the accuracy IMPROVEMENT after each level starting from the basic model
- Remove one component at a time and see how accuracy drops



Types of ML

Classification

- Logistic Regression
- Decision Tree
- AdaBoost
- Naive Bayes Classification
- SVM (Support Vector Machine)





Types of Learning

Supervised: Learning by Labelled Ex

- Eg. Face Recognition
- Amazingly effective if you have labelled examples

Unsupervised: Discovering Patterns

- Eg. Google News Data Clustering
- Useful if you lack labelled data

Reinforcement: Feedback right/wrong

- Eg. Playing chess by winning or losing
- Works well in some domains, becoming more important

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Machine learning workflow



Unsupervised Learning

K-means Clustering



K = 2

K = 4







https://www.datascience.com/blog/k-means-clustering

Unsupervised Learning

• Clustering





Reinforcement Learning

How does a Human learn?

- Tilt the bike in 0 deg: Goes out of Fence
- Tilt it in 90 deg: Loses balance and falls down
- Getting these feedback / reward, learn how to ride i.e, learn the angle




Reinforcement Learning



Soliton

https://www.datascience.com/blog/k-means-clustering

Reinforcement Learning





MOOC for ML

cs229 is good place to start

Do a lot of assignments

Work on pet projects

Contribute to ML Open source libraries

Courses

- ML: cs229 by Andrew Y. Ng
- RL: <u>David Silver</u>

Books:

Blogs & Github:

- Scikit-Learn examples
- <u>ML Playground</u>



How to Solve this?

We MAY be able to solve this by introducing one more feature which MAY separate them linearly.

Or I will let SVM project it to higher dimension and find hyperplane and reproject it back

Do you see any pattern? Any mathematical solution?





Clue..!

Think in MATHEMATICS..!





















What is Next?

Let the Algorithm Learn these

- Functions
- Features

ON ITS OWN...!

Deep Learning





Lunch Break

Feed yourselves well to feed the Machines more..!

Day 2 - AN 1 (DL)

What is the limitation of simple Image Processing and why we need intelligent systems?

What we know from Neuroscience

- Layer wise processing
- Hierarchical
- Simple Cells -> Complex Cells
- Closest Analog: IT
- Fovea
- Fusion of other sensory i/p
- Generative Model of world
- Even V1 gets feedback from
- Feedforward IT ~ CNN
- (role of feedback)



Limitation of Traditional ML

- Need to hand engineer features which can take a lot of time
- The limitations in its ability to represent complex features (Requires a lot of diligence and intelligence)
- Models developed for one problem cannot be easily be utilised for a similar problem



Simplest Models Perceptron vs. the point neuron

- Incoming signals from synapses are summed up at the soma
- $^{\Delta}$, the biological "inner product"
- On crossing a threshold, the cell "fires" generating an action potential in the axon hillock



The McCulloch and Pitt's neuron



Synaptic inputs: Artist's conception





Simplest Models

• Perceptron training

Include bias term as the third weight(w3) with its input always set to 1 Step 1: Initialization: $w_i = 0$, i = 1 to n For each of the training sample do steps 2 -4 Step 2: Compute output by weighted linear combination of inputs (Vi = w1 *x1 + w2 * x2 + 1 * bias) Step 3: Find the error (Error = Anticipated output - predicted output) Step 4: Update each weight based on the following $\Delta Wi = Error * \Im * Xi$ $Wi = Wi + \Delta Wi$ Where \Im is the learning rate and its range is $0 \le \Im \le 1$

Step 5: Repeat the procedure until no error results



Enough Talk..! Let's Code!!

IPython Notebook

Perceptron Limitations - Linear separability

- A simple perceptron cannot learn a classifier for a XOR gate
- How to draw a decision boundary in case of a XOR gate?



Problem of Linear separability

Linear vs. nonlinear problems



- Can this kind of perceptron provide solutions to all kinds of data patterns we might encounter in practice? <u>Let's find</u> out
- This is because we don't have non-linear elements in our network. Hence, this kind of network can only learn linear functions of inputs.
- How can we improve the network to learn non-linear functions?
- Key observation Cannot directly classify data. Convert the data to a new feature space to classify
- Nonlinearities should be included in the network

Sigmoid activation function

- We can include non-linear functions in our to improve the representational power of the network.
- We know how a initial models of how neuron fires.



• Can we represent this kind of activation as continuous and smooth function

• The sigmoid function is shown as follows



- Here x is weighted combination of the neuron inputs.
- The neuron fires when x >> 0 and does not fire when x << 0. The neuron lies in a transition state when when x ≈ 0.
- The function is smooth and differentiable

Case of two layers with non-linearities - MLP - The perceptron revenge

- Convert the inputs into a new feature space where the data points are linearly separable
- This necessitates the need at least two neurons with non-linearities. This kind of architecture is called Multilayer Perceptron (MLP)
- The first layer is called input layer, the layer at the last is called output layer. The layer / layers in between are called hidden layers



MLP

- A simple Multilayer network will consist of an input layer, output layer and one or more hidden layer in between
- It is not necessary that each hidden layer should contain same number of neuron. Each hidden layer usually contains a non-linear activation function



But what about training?

- In a single layer perceptron, there was direct interaction between input and output, hence we were able to update their weights directly based on output and inputs.
- Training becomes a little harder in MLPs, since we there are multiple layers of weight.
- We will measure the error committed by the network through an objective function (Just measure the squared difference between the anticipated output and predicted output MSE)
- We will then try to find the minima of the objective function through gradient descent
- But how do we update weights of the network based on direction to move in gradient descent?



MLP - Backpropagation

- Backpropagation provides a way to compute the gradient of the error function with respect to each of the weights in the network.
- This provides a way to update update the weights of the network based on the error function.







Terminologies:-

C - cost function

a_i^L- jth neuro

 $\delta_{j}^{J_{L}}$ - error of the jth neuron in the Lth layer

 b_j^{i} - bias of the jth neuron in the Lth layer

 w_{jk}^{I} - weight connecting the jth neuron in the Lth layer to kth neuron in the L-1th layer

$$\delta_j^L = \frac{\partial C}{\partial a_j^L} \sigma'(z_j^L).$$

$$\delta^l = ((w^{l+1})^T \delta^{l+1}) \odot \sigma'(z^l),$$

 $\frac{\partial C}{\partial b_j^l} = \delta_j^l.$



Representational power of MLP

- Can this kind of MLP learn any functions?
- It turns out that this kind of neural network with one hidden layer is a universal approximator i.e., these neural networks can model any continuous function.
- Then why are many hidden layers required?
- It is practically difficult to learn the exact values of the parameters in such networks. Hence multiple layers make it practically possible to exploit the representational power of a neural network.



MLP - Limitations

- Very expensive training process (Too many parameters to learn)
- Not scalable to a larger architecture. The number of neurons increases rapidly with the number of neurons in the network.
- Does not converge

What do Neural Networks Learn?





CNN

- Neurons are arranged in a 3D layer, unlike a MLP, where it is arranged in a 2D layer
- Each neuron views only a specific portion of the input and shares its parameters with many neurons in the same layer
- Encodes properties that are more desirable for images.
- Convolutional neural networks calculate the output from the input by repeated applying convolution operation.



Convolution - signals motivation

Continuous case



convolution is a mathematical operation on two functions to produce a third function giving the summation of the pointwise multiplication of the two functions as one of the functions is translated throughout

$$egin{aligned} (fst g)[n] &= \sum_{m=-\infty}^\infty f[m]g[n-m] \ &= \sum_{m=-\infty}^\infty f[n-m]g[m]. \end{aligned}$$

Discrete case



Convolution

1D





3D

....

0	0	0	0	0	0	 0	0	0	0	0	
0	156	155	156	158	158	 0	167	166	167	169	1
0	153	154	157	159	159	 0	164	165	168	170	1
0	149	151	155	158	159	 0	160	162	166	169	1
0	146	146	149	153	158	 0	156	156	159	163	1
0	145	143	143	148	158	 0	155	153	153	158	1
	Inpu	t Cha	innel	#1 (Red)	1	nput	Char	nel ‡	‡2 (G	re
	Γ	-1	-1	1	1		ſ	1	0	0]
		0	1	-1	1			1	-1	-1	1
		0	1	1	1			1	0	-1	
	Ke	ernel	Char	nel ‡	<i>‡</i> 1		Ke	rnel	Char	nel ‡	‡2
			Ţ						Û		

+

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-498

0	0	0	0	0	0	
0	163	162	163	165	165	
0	160	161	164	166	166	
0	156	158	162	165	166	
0	155	155	158	162	167	
0	154	152	152	157	167	
1						
	Input	Cha	nnol	#2 (Rhugh	-

Input Channel #3 (Blue)

1	0	1	1
	0	1	0
	1	-1	1

Kernel Channel #3

+



....

----.... ----

Convolution





Convolution by Neurons



Convolution

ZERO PADDING - zeros can be added to the feature map to increase the size of the feature map. The idea is to keep the size of the feature map the same throughout

STRIDES - Number elements that should be skipped in the feature map while doing convolution

Zero Padding



Convolution on a feature map with three different strides



What does deep learning learn?

- MLPs without bias term model linear transformation
- MLPs with bias term model affine transformation
- The activation functions introduces further non-linearities
- Deep learning learns a transformation of a feature space that becomes linearly separable in a different topological space
- Link <u>convnetjs</u>

Deep Learning







Problem with tanh layer /sigmoid

- The tanh/ sigmoid activation function squashes a real number in between zero and one
- It involves expensive operations, hence slows down the training process
- Its output saturates at both ends, hence produces "vanishing gradient problem" i.e., the gradient becomes zero at these saturation points and the network cannot learn weights based on backpropagation



ReLU

- Does not saturate at extremes, hence allow gradients to propagate through larger networks
- Sparse activations A characteristic property of biological neurons
- ReLUs are computationally inexpensive.
- Though Relu's gradient is undefined at x=0, it is not practically a huge concern







Other layers

Pooling layer - Down samples the size of feature map. Promotes translation invariance



Dropout layer - Randomly removes a few neurons in the connection. Reduces overfitting





Data Preprocessing

Does not improve accuracy generally. But improves the speed of training







CNN



FC / Fully connected layer:-

- The neurons in the normal layers in CNNs are not connected to all neurons of the previous layer. But towards the end of the network, all neurons in a layer are connected to all neurons in the previous layers.
- This layer increases the representational power of the network but involves more parameters than a convolutional layers
- This layer is very useful for making classification decision based on the learnt feature maps. Fully connected layer gives the power to a neuron to mix all features of the previous layer, which is not possible with convolution.
- The last fully connected layer does the function of a SVM or softmax
CNN: What Changed

ILSVRC



Li Fei-Fei: ImageNet Large Scale Visual Recognition Challenge, 2014 http://image-net.org/

- ReLU
- Shared Weights
- Specialized Layers: CP
- GPGPU
- Availability of OSS Libraries/Datasets



Overfitting





Overfitting increases with number of neurons. But it is not a good practice to decrease the number of neurons but to use regularisation

Regularisation



Regularisation helps to generalise to the given data while maintaining the representational power of the network

Types of regularisation:-

- L1 regularisation Prefers sparse distribution
- L2 regularisation heavily penalizes peaky weight vectors and prefers more diffuse weight vectors.
- Combination Combination of both



HYPERPARAMETER STRATEGIES

- Hyperparameters are parameters which are not learned by the algorithm but should be manually fixed empirically. Deep learning involves several hyperparameters like learning rate, batch size, size of convolution, stride etc..
- First do a coarse search with small epochs and fine search with larger epochs
- If the best value for a hyperparameters occurs in the border of an interval, do a double check by trying values beyond the boundary so that so you don't miss out on the optimal hyperparameter
- Don't do grid search, always prefer random search



Impact of deep in ILSVRC

ILSVRC



Li Fei-Fei: ImageNet Large Scale Visual Recognition Challenge, 2014 http://image-net.org/

ALEXNET - The gamechanger



Impact of deep in ILSVRC



Alexnet architecture details

It consists of 8 layers - 5 convolutional layers and 3 fully connected layers. AlexNet



Residual Networks

Counterintuitively, error increases with increase in depth beyond a certain point

The idea of skip connection suggests that it is easier to learn minor modifications to identity functions









Google net

3x3 max pooling

Concat Dropout Fully connected

Softmax

5x5 convolutions

Filter

3x3 convolutions

Previous layer

1x1 convolutions

- The biggest contribution from google net was the introduction of inception module - A module where features from multiple layers can be mixed together
- Inception provides a way for combining local and global features

Spatial Transfer Networks (STN)

- Introduces a network to make images invariant to rotations and translations
- It consists of a localisation network that computes the spatial transformation, creation of sampling grid through a grid generator and a sampler which warps the input based on the generated grid.
- Link for <u>STN</u>





Autoencoders

- Autoencoder is a network which is typically used to learn a fixed number of features that can best represent the data
- This type of networks can be used for data compression





Recurrent Neural Network

Unlike feedforward neural network, RNN can have loops.

Useful for Sequential inputs.

Useful in applications where memory about the past output can play a role in predicting the current output



Visualization examples

Techniques:-

- 1. Layer activations
 - a. Visualise the activations of the network. When we use ReLU, the activations starts out relatively blobby but spreads out during learning.
 - b. Some activations may be all zero indicating high learning rate.
- 2. Visualise weights
 - a. Weights are the most interpretable on the first layer, which is looking at the input pixels directly.
 - b. Weights from other layers can be visualised too. They will usually form some smooth patterns. Noisy patterns indicate that the network has not probably learnt well and needs to trained longer.
- 3. Retrieving images that maximally excite a neuron.
 - a. A large dataset of images is taken. The images which fired maximally for some neuron are recorded. Hence this will give us a good insight into what the neuron has learnt.
 - b. One problem with this is that each Relu neuron might not learn something sematic. It is the combination of several Relu neurons that learn something semantic.

Visualization examples

4. Low dimensional embedding :-

Several visualisation techniques have been proposed which convert the image vectors in high dimensional space to a 2-D space, preserving the pairwise distance between any two points. The best known technique is tsne- Embedding

5.Occluding parts of image (for classification):-

We can set a patch of the image to be all zeros. We can iterate position of the patch throughout the image and record the probability of correct class label as a function of position. A 2-dimensional heat map can be produced through such procedure. The probability should reduce considerably at position where the actual object is placed in the image.

Be careful with DATA









Nuts

Challenges (GPU for Training)



